



## 1<sup>st</sup> Gas Dynamics Report

**مطلوب حل التقرير بخط اليد** وعدم استخدام الحاسب (أى تقرير بالحاسب أو الإجابات المنقولة أو المصورة درجتها ستكون صفر) **تعديل موعد تسليم التقرير بعد 4 أسابيع من تاريخه (محاضرة الثلاثاء 12 مارس 2024) ولن يتم قبول أى تقرير بعد الموعد.**

1- Find what is wrong in each of the following statements and then re-write the full correct statement (you can also add a T-S diagram to show the correct meaning) :

- In Gas Dynamics, we define Mach number in a C-D nozzle as a constant thermodynamic property which is equal to  $(a/V)$  where  $a$  is the vector of the gas velocity.
- In Gas Dynamics, we have to assume that Mach number is  $\geq 0.3$  all the time and assume also that the speed of sound through all gases is equal to 342 m/s all the time.
- If air velocity in C-D nozzle is less than 0.3 speed of sound we must assume the flow is isentropic and incompressible and must assume also that the air is a thermal perfect gas.
- The speed of sound in a subsonic air flow in C-D nozzle remains constant if the flow is accelerated to a supersonic flow because we assume air is a thermal perfect gas.
- In Isentropic flow in a converging nozzle, the flow is isentropic and the exit properties must be sonic properties for any value of back pressure and any length of the nozzle.

2- Define the physical meaning and the mathematical equation for calculating the speed of sound,  $a$ , in any gas. What are the assumptions we make to get that equation? Can we calculate the speed of sound for a gas if it is moving at  $M=1$  or it is moving at  $M > 1$ ?

3- Find what is wrong in each of the following statements and then re-write the full correct statement (you can also add a T-S diagram to show the correct meaning) :

- We cannot define the speed of sound for any incompressible flow because the density is must assumed to be constant and because the Mach Number is less than 0.3.
- We can define the speed of sound,  $a$ , for air only and we have to assume the speed of sound a scalar quantity because it moves in the  $x$ -direction only.
- For an incompressible flow, the speed of sound is defined as propagation of huge pressure pulse through isothermal fluid where friction and heat transfer are neglected.
- All fluids at the same temperature must have the same speed of sound because the speed of sound is a function of the temperature only.
- In a converging nozzle, the flow is isentropic and the exit properties must be sonic properties for any back pressure and any length of the nozzle.

4- Given that  $dA/A = (1-M^2)(dp/\rho V^2) = - (1-M^2)(dV/V)$ , Show that the converging-diverging nozzle is the only possible shape though which a gas may be accelerated smoothly from subsonic flow to supersonic flow without violating any of the gas dynamics relations. (use any needed equations and sketches).

5- Define the physical meaning of the speed sound. If we found that  $a^2 = (\partial p / \partial \rho)$ , show that the speed of sound in a thermally perfect gas is  $a = \sqrt{\gamma RT}$  (if we assume that sound waves are propagating isentropically). Prove that the speed of sound in a thermally perfect gas is  $a = \sqrt{RT}$  (if we assume sound waves are propagating isothermally not isentropically). Which value is more accurate:  $(a = \sqrt{\gamma RT})$  or  $(a = \sqrt{RT})$  ? why ?

6- What is the "Mach Cone"? Define the physical meaning and the mathematical equation for calculating the half angle,  $\alpha$ , of that cone. Can we see the Mach cone in a liquid or in an incompressible fluid ?



7- Define the physical meaning and the mathematical equations for the total isentropic stagnation properties ( $P_o$ ,  $T_o$ ,  $h_o$ , etc) and the critical isentropic properties ( $P^*$ ,  $T^*$ ,  $h^*$ , etc). Show both types of properties on T-S chart if the flow is subsonic and if it is supersonic.

8- Discuss, using the mass conservation, both the physical meaning and the mathematical relations which describe the choking (الإختناق) in a variable area channel. Where may choking take place? and How? What are the conditions that must exist to have a choking? What are the possible flow conditions downstream of the choked area?

9- Find what is wrong in each of the following statements and then re-write the full correct statement (you can also add a T-S diagram to show the correct meaning) :

- All stagnation isentropic conditions ( $P_o$ ,  $T_o$ ,  $h_o$ , etc) of any subsonic flow must change if the flow becomes sonic or supersonic through an isentropic process.
- All stagnation isentropic conditions ( $P_o$ ,  $T_o$ ,  $h_o$ , etc) of any subsonic flow must change if the flow becomes sonic or supersonic through a non-isentropic process.
- All critical isentropic conditions ( $P^*$ ,  $T^*$ ,  $h^*$ , etc) of any subsonic flow must change if the flow becomes sonic or supersonic through an isentropic process.
- All critical isentropic conditions ( $P^*$ ,  $T^*$ ,  $h^*$ , etc) of any subsonic flow must change if the flow becomes sonic or supersonic through a non-isentropic process.
- For flow in a converging nozzle, the flow is isentropic and the exit properties must be sonic properties for any back pressure and any length of the nozzle.

10- What is the temperature, density,  $\rho$ , pressure,  $p$ , and speed of sound,  $a$ , on the nose of a supersonic fighter flying at a Mach number of  $M=2$  through air at 273K and 0.7 bar.

11- Find what is wrong in each of the following statements and then re-write the full correct statement (you can also add a T-S diagram to show the correct meaning) :

- All perfect gases of the same value of  $\gamma$  will have the same stagnation conditions ( $P_o$ ,  $T_o$ ,  $h_o$ , ...etc) and also the same critical conditions ( $P^*$ ,  $T^*$ ,  $h^*$ , ...etc).
- Two perfect gases with different values of  $\gamma$  can not have the same stagnation conditions ( $P_o$ ,  $T_o$ ,  $h_o$ , ...etc) and also the same critical conditions ( $P^*$ ,  $T^*$ ,  $h^*$ , ...etc).
- In calculating reference stagnation properties ( $P_o$ ,  $T_o$ ,  $h_o$ , etc) we get an adiabatic decrease in both of gas temperature and density but we get an increase in the gas pressure.
- Inside the Mach Cone created by the subsonic flow of an airplane, the speed of sound must be constant because we assume air is a thermal perfect gas.
- In Compressible flow in a converging nozzle, the flow is isentropic and the exit properties must be sonic properties for any back pressure and any length of the nozzle.

12- Air from a large tank flows at  $M=0.5$  through a conduit of a cross-sectional area of  $65\text{cm}^2$ . The conditions in the tank are 340 kPa, abs. and  $10^\circ\text{C}$ . Calculate the properties,  $P$ ,  $T$ ,  $\rho$ ,  $a$ , and the mass flow rate through that cross-section of the conduit.

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